

## A statistical analysis of the interaction between grain boundary and forest hardening

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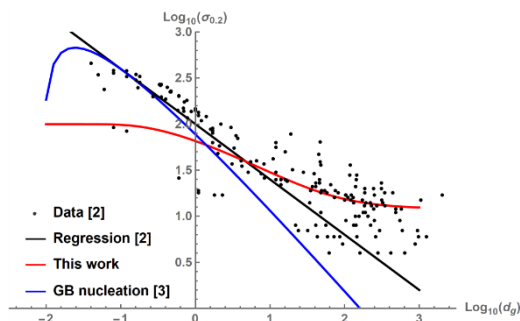
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The grain size effect (GSE) is generally described by a relationship between the yield strength  $\sigma_y$  and grain size  $d_g$  as  $\sigma_y = \sigma_0 + k_{HP}d_g^{-n}$ . For  $n=1/2$ , this is the Hall-Petch relationship, generally explained by the formation of dislocation pileups at grain boundaries (GBs) [1]. A large set of experimental data [2] shows  $n \neq 1/2$  for most metals and a large dispersion of the data with respect to the regression formula.

For a dislocation density  $\rho_d=10^{12} \text{ m}^{-2}$ , the average number of dislocation segments per grain falls below 1 at a value of  $d_g \approx 2.5 \cdot 10^{-6} \text{ m}$ , precluding the effect of dislocation pileups [3]. The present work demonstrates this transition trough a mathematical analysis of the probability of storage and annihilation at GB and forest sites, based on the slip length concept proposed in the Kocks-Mecking model [4].

The  $\sigma_y$ - $d_g$  curves are extrapolated from model fits to sets of tensile tests for different  $d_g$ . No fitting parameter for  $d_g$  is used. For  $d_g < 10^{-7} \text{ m}$ , the stress required to activate a GB dislocation source becomes more important than the slip length effect. The combination of the statistical analysis with the mechanistic approach for ultrafine grains [3] provides a consistent explanation for the GSE.

**Keywords:** Kocks-mecking; Hall-Petch; Dislocation forest; Grain boundary source



**Fig. 1.** Predicted  $\sigma_y$ - $d_g$  curve based on tensile tests for aluminium with different grain sizes (red) and nucleation stress for grain boundary dislocations (blue) [3], compared to the dataset and regression curve Eq. (1) provided by Cordero et al. [2].

### References:

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